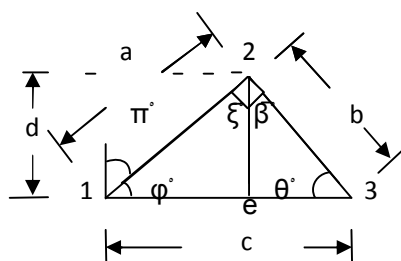


إثبات نظرية فيثاغورس باستخدام الجيب والجتا وتطابق الزوايا

نظرية فيثاغورس : $c^2 = a^2 + b^2$



$$\Delta 123 \quad \cos \varphi^\circ = \frac{a}{c}$$

$$\Delta 12e \quad \cos \varphi^\circ = \frac{1e}{a}$$

$$\text{But } \cos \varphi^\circ = \cos \varphi^\circ$$

$$\therefore \frac{a}{c} = \frac{1e}{a} \leftrightarrow a^2 = 1e \times c \quad \dots\dots \text{eq}^{\underline{n1}}$$

$$\text{And } \pi^\circ + \varphi^\circ = 90^\circ, \xi^\circ + \beta^\circ = 90^\circ$$

$$\text{but } \pi^\circ = \xi^\circ \text{ بالتناظر}$$

$$\therefore \varphi^\circ = \beta^\circ$$

$$\Delta 123 \quad \sin \varphi^\circ = \frac{b}{c}$$

$$\Delta e23 \quad \sin \beta^\circ = \frac{e3}{b}$$

$$\therefore \frac{b}{c} = \frac{e3}{b} \leftrightarrow b^2 = e3 \times c \quad \dots\dots \text{eq}^{\underline{n2}}$$

$$\text{Add } \text{eq}^{\underline{n1}} + \text{eq}^{\underline{n2}}$$

$$a^2 = 1e \times c$$

+

$$b^2 = e3 \times c$$

$$a^2 + b^2 = 1e \times c + e3 \times c \leftrightarrow c(1e + e3)$$

$$\text{But } (1e + e3) = c$$

$$a^2 + b^2 = c (c)$$

$$\therefore c^2 = a^2 + b^2$$